

6.3 Binomial Random Variables continued

#79, 81, 83

$$79. \text{ a. } P(X = 17) = \binom{20}{17} (.85)^{17} (.15)^3 = 0.2428$$

$$\text{ b. } P(X < 12) = \binom{20}{0} (.85)^0 (.15)^{20} + \dots + \binom{20}{12} (.85)^{12} (.15)^8$$

= 0.0059. This is low. Judy should be suspicious.

$$81. \text{ a. } \mu_x = 15(0.20) = 3$$

If we watched the machine make sets of 15 calls, we would expect about 3 calls to reach a live person, on average.

$$\text{ b. } \sigma_x = \sqrt{15(0.20)(0.80)}$$

= 1.55. If we watched the machine make many sets of 15 calls, we would expect the number of calls that reach a live person to typically vary by about 1.55 from the mean of 3.

83. a. $\mu_y = 15(0.80) = 12$

Notice that $\mu_x = 3 \dots$ and $12 + 3 = 15$ (total # of calls)

b. $\sigma_y = \sqrt{15(0.80)(0.20)}$
 $= 1.55$

This is the same value as σ_x because $Y = 15 - X$ and adding a constant to a random variable doesn't change the spread.