

57. **Vertical Motion** The velocity of a ball thrown vertically upward from ground level is given by  $v(t) = -32t + 48$ , where  $t$  is the time in seconds and  $v$  is the velocity in feet per second.

- Find the velocity when  $t = 1$ .
- Find the time when the ball reaches its maximum height. [Hint: Find the time when  $v(t) = 0$ .]
- Find the velocity when  $t = 2$ .

58. **Dimensions of a Rectangle** A wire 24 inches long is to be cut into four pieces to form a rectangle with one side of length  $x$ .

- Express the area  $A$  of the rectangle as a function of  $x$ .
- Determine the domain of the function and use a graphing utility to graph the function over that domain.
- Use the graph of the function to approximate the maximum area of the rectangle. Make a conjecture about the dimensions of the rectangle.

In Exercises 59–62, let  $f(x) = 3 - 2x$ ,  $g(x) = \sqrt{x}$ , and  $h(x) = 3x^2 + 2$ . Find the indicated value.

59.  $(f - g)(4)$                       60.  $(fh)(1)$   
 61.  $(h \circ g)(7)$                       62.  $(g \circ f)(-2)$

In Exercises 63–66, (a) find  $f^{-1}$ , (b) sketch the graphs of  $f$  and  $f^{-1}$  in the same coordinate system, and (c) verify that  $f^{-1}(f(x)) = x = f(f^{-1}(x))$ .

63.  $f(x) = \frac{1}{2}x - 3$                       64.  $f(x) = 5x - 7$   
 65.  $f(x) = \sqrt{x + 1}$                       66.  $f(x) = x^3 + 2$

In Exercises 67–70, find a mathematical model representing the statement. (In each case, determine the constant of proportionality.)

- $F$  is jointly proportional to  $x$  and the square root of  $y$ . ( $F = 6$  when  $x = 9$  and  $y = 4$ .)
- $R$  varies inversely as the cube of  $x$ . ( $R = 128$  when  $x = 2$ .)
- $z$  varies directly as the square of  $x$  and inversely as  $y$ . ( $z = 16$  when  $x = 5$  and  $y = 2$ .)

70.  $w$  varies jointly as  $x$  and  $y$  and inversely as the cube of  $z$ . ( $w = \frac{44}{9}$  when  $x = 12$ ,  $y = 11$ , and  $z = 6$ .)

71. **Domestic Motor Fuel Consumption** The table gives the average fuel consumption  $y$  in miles per gallon for cars in the United States at 5-year intervals from 1970 through 1990. The time in years is given by  $t$ , where  $t = 0$  represents 1970. (Source: U.S. Highway Administration)

$t$	0	5	10	15	20
$y$	13.52	13.52	15.46	18.20	21.02

- Find the least squares regression lines for the data.
- Sketch a scatter plot of the data and graph the linear model you found in part (a) on the same set of axes.
- Interpret the slope of each model in the context of the problem.
- Use the model to estimate average fuel consumption for the year 2000.

72. **Average Hourly Wage** The table gives the average hourly wages ( $y_1$ ) for workers in the mining industry and the average hourly wages ( $y_2$ ) for workers in the construction industry in the United States for the years 1990 through 1993. The time in years is given by  $t$ , where  $t = 0$  represents 1990. (Source: U.S. Bureau of Labor Statistics)

$t$	0	1	2	3
$y_1$	\$13.68	\$14.18	\$14.51	\$14.60
$y_2$	\$13.77	\$13.99	\$14.11	\$14.35

- Find the least squares regression lines for mining wages versus time and construction wages versus time.
- Sketch a scatter plot of the data and graph the linear models you found in part (a) on the same set of axes.
- Interpret the slope of each model in the context of the problem.
- Use the models to estimate the wages in each industry for the year 2000.

