Finance Math

## Part 1: Algebra Skills

1. Simplify: $\left(5 x^{2}-6 x-9\right)+\left(8 x+2 x^{2}+3\right)$
2. Multiply: $\left(5 y^{3} z^{5}\right)\left(-3 x y^{3} z^{4}\right)$
3. Multiply: $(3 a+5)(3 a-7)$
4. Solve the following system of equations for x .

$$
\begin{aligned}
& x+3 y=1 \\
& 5 x-3 y=-25
\end{aligned}
$$

5. Solve the following system of equations for $y$.

$$
\begin{aligned}
& 4 x+3 y=9 \\
& 2 x+5 y=8
\end{aligned}
$$

6. Simplify: $\left(-3 x^{-3}\right)^{-2}$
7) Subtract: $\left(5 x^{2}+7 x\right)-\left(3 x^{2}-x+9\right)$
8) Find a factor of $4 x^{2}-25 x-21$.
9) Multiply. $\frac{15 x^{2} y^{3}}{8 x y} \cdot \frac{24 x^{2}}{5 x y^{5}}$

Use $f(x)=3 x^{2}-2 x+5$ and $g(x)=4 x-2$ for problems 10-13.
10) Find $f(2)-g(4)$.
11) Find $g(f(x))$.
12) Find $g(f(-4))$
13) Find $f(g(x))$
14. What is the vertex of $y=x^{2}-4 x+3$ ?
15. Solve $2 x^{2}+5 x-12=0$.
16. Write in lowest terms: $x^{2}-4 x-12$

$$
\frac{x^{2}-4 x-12}{x^{2}-9 x+18}
$$

17. Graph. Is $(1,0)$ a solution to this system of linear inequalities?

$$
\begin{aligned}
& 3 x+4 y<12 \\
& y<1 / 2 x+5 \\
& y>-3
\end{aligned}
$$

18. Find the solution(s) of $y=2 x^{2}-3 x-35$

## Part II: Compound Interest

19. After 6 months of investing, your portfolio has a value of $\$ 10,600$. You started with $\$ 9,000$. What is the percentage increase in your portfolio?
20. You bought 600 shares of Microsoft Corporation 5 weeks ago at $\$ 25.15$ per share. Today the share price is $\$ 20.65$. How much money have you lost?
21. An amount of $\$ 1,750.00$ is deposited in a bank paying an annual interest rate of $5.7 \%$ compounded quarterly. Find the balance after 4 years.
22. An amount of $\$ 5,000.00$ is deposited in a bank paying an annual interest rate of $6 \%$ compounded daily. Find the balance after 3 years.
23. An amount of $\$ 4,500.00$ is deposited in a bank paying an annual interest rate of $3.7 \%$, compounded continuously. Find the balance after 4 years.
24. Give an example of converting an exponential form equation to logarithm form.

$$
a^{x}=b
$$

25. How long would it take to double $\$ 600$ at $6.2 \%$ annual interest compounded annually?
26. You are purchasing a car for $\$ 18,000$ at $5.2 \%$ interest and financing this purchase over a period of 5 years. What would be your monthly payment?

## Part III: Investing and Budgeting

27. GloboGym Corporation has a stock price of $\$ 3$ on $1 / 1 / 2000$. On $1 / 1 / 2012$, the price was $\$ 9$. Find an equation of the line in slope-intercept form that represents a linear progression of the stock price.
28. You bought a new car 6 years ago. This car loses all marketable value after 10 years. If the purchase price was $\$ 17,000$, how much is it worth today? (Assume straight-line depreciation)
29. What would be the monthly payment on a car that costs $\$ 18,500$ plus $7.6 \%$ sales tax financed over 5 years at $4 \%$ interest?
30. How much would you be financing (borrowing) on a car purchase of $\$ 16,600$ plus $6.9 \%$ tax, followed by a $\$ 3,000$ cash down payment?
31. You go to breakfast with friends and pay the bill. The check comes to $\$ 49.50$ plus $6.6 \%$ sales tax. You give an $14 \%$ tip. How much does the meal cost you?
32. Factor $2 x^{2}-7 x-9$
33. Factor and Solve: $y=4 x^{2}+19 x-5$
34. You bought a car 5 years ago. This car loses historically has depreciated at a rate of $10.5 \%$ per year (assuming exponential depreciation). If the purchase price was $\$ 15,000$, how much is it worth today?
35. You are purchasing a 3 year-old used car. If the current price is $\$ 16,500$ and has historically depreciated at a rate of $8 \%$ per year, how much did the car cost when it was new? (assume exponential depreciation).
36. You have a 5 year old car that is worth $\$ 12,400$. It originally sold for $\$ 16,600$ when it was new. What is the average rate of depreciation for this vehicle? (assume exponential depreciation).
37. You bought a new car for $\$ 17,500$. The historical depreciation rate for this particular car has been $11 \%$ per year (assume exponential depreciation). In how many years will this car be worth $\$ 10,000$ ?
38. Conduct a breakeven analysis on the following functions to determine a pricing structure.

Cost Function: $C(x)=4 x+600$
Revenue Function: $R(x)=-x^{2}+81 x-80$

You bought a new car for $\$ 18,500$. There is $6.9 \%$ sales tax and you can get a $4.1 \%$ interest rate to finance this car over a 4 year period. You have decided to include a $\$ 2000$ down payment (after taxes). The car historically depreciates at a rate of $10 \%$ per year.
39. How much tax will you be paying on this car?
40. What is your monthly payment?

